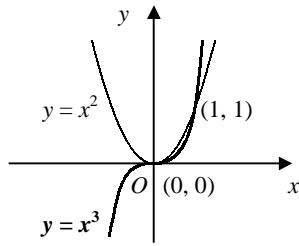
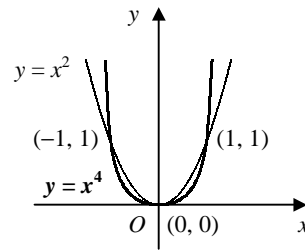


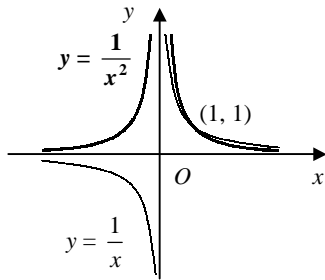
1 a



b

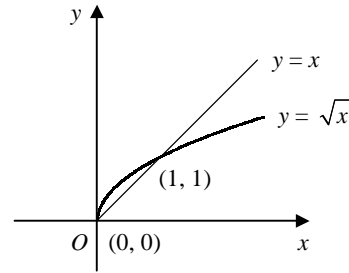


c

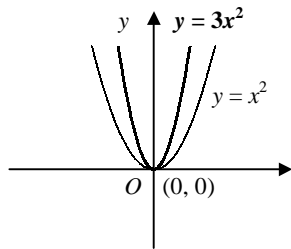


asymptotes: $y = 0$ and $x = 0$

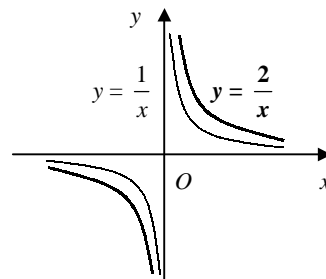
d



e



f

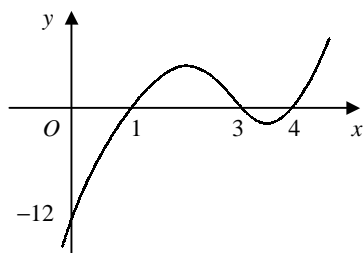


asymptotes: $y = 0$ and $x = 0$

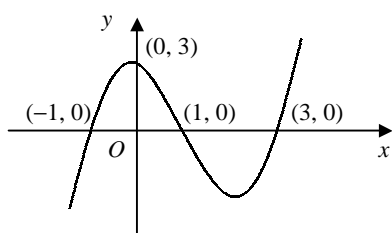
2 a $= (-1) \times (-3) \times (-4) = -12$

b $x = 1, 3, 4$

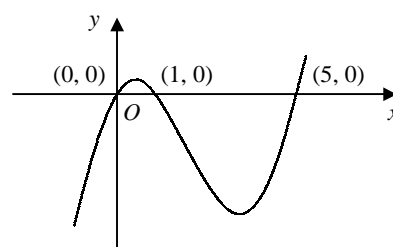
c

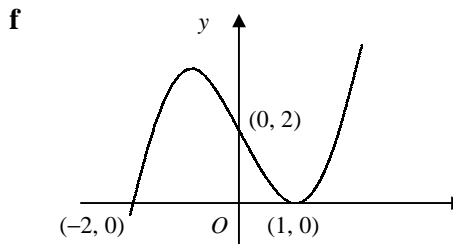
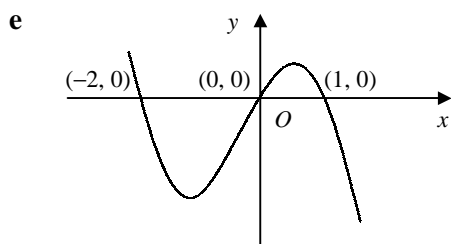
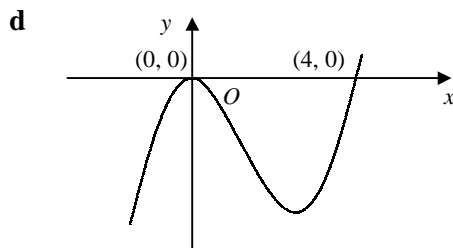
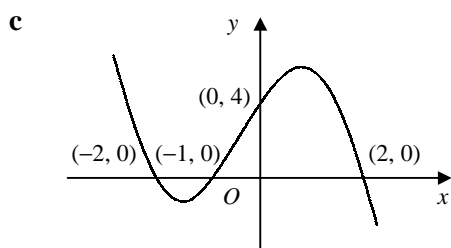


3 a

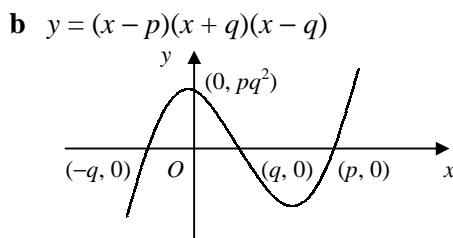
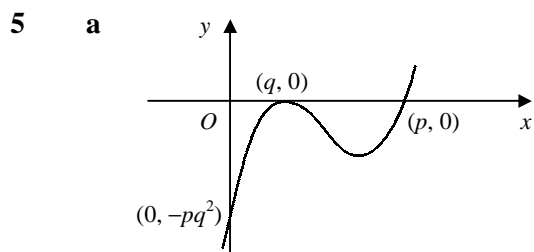
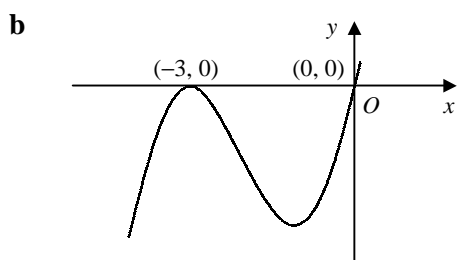


b





4 a $= x(x^2 + 6x + 9) = x(x + 3)^2$



6 TP at $(1, -2)$
 $\therefore f(x) = k(x - 1)^2 - 2$
 crosses y-axis at $(0, -5)$
 $\therefore -5 = k - 2$
 $k = -3$
 $\therefore f(x) = -3(x - 1)^2 - 2$
 [$f(x) = -3x^2 + 6x - 5$]

7 crosses x-axis at $(-2, 0)$, $(1, 0)$ and $(2, 0)$
 $\therefore y = k(x + 2)(x - 1)(x - 2)$
 crosses y-axis at $(0, -8)$
 $\therefore -8 = 4k$
 $k = -2$
 $\therefore y = -2(x + 2)(x - 1)(x - 2)$
 $= -2(x + 2)(x^2 - 3x + 2)$
 $= -2(x^3 - 3x^2 + 2x + 2x^2 - 6x + 4)$
 $= -2x^3 + 2x^2 + 8x - 8$
 $\therefore a = -2, b = 2, c = 8, d = -8$

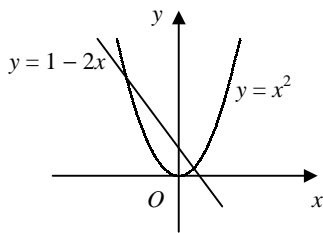
8 a 4

b 0

c 2

d 3

9 a



b 2 roots as $x^2 + 2x - 1 = 0 \Rightarrow x^2 = 1 - 2x$ and the graphs of $y = x^2$ and $y = 1 - 2x$ intersect at 2 points

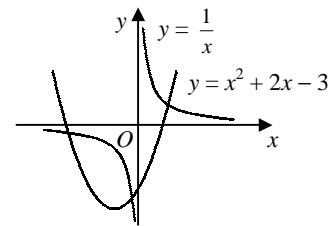
10 a $x^2 + 2x - 3 = (x + 1)^2 - 1 - 3 = (x + 1)^2 - 4 \therefore$ turning point is $(-1, -4)$

b $x^2 + 2x - 3 - \frac{1}{x} = 0 \Rightarrow x^2 + 2x - 3 = \frac{1}{x}$

\therefore roots where $y = x^2 + 2x - 3$ and $y = \frac{1}{x}$ intersect

graphs intersect at 1 point for $x > 0$ and 2 points for $x < 0$

\therefore one positive and two negative real roots



11 $x - 3 = x^2 - 5x + 6$

$$x^2 - 6x + 9 = 0$$

$$(x - 3)^2 = 0$$

repeated root

$\therefore y = x - 3$ is tangent to $y = x^2 - 5x + 6$

12 a $x^2 + 5x + 8 = 3x + 7$

$$x^2 + 2x + 1 = 0$$

$$(x + 1)^2 = 0$$

$$x = -1 \therefore x = -1, y = 4$$

b repeated root

$\therefore y = 3x + 7$ is tangent to $y = x^2 + 5x + 8$ at the point $(-1, 4)$

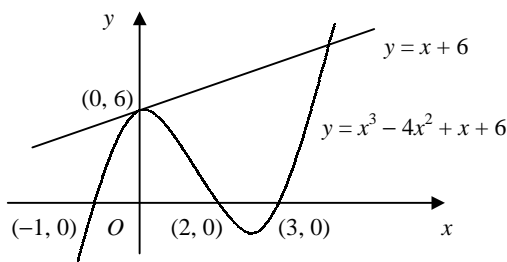
13 a $x^3 - 4x^2 + x + 6 = x + 6$

$$x^3 - 4x^2 = 0$$

$$x^2(x - 4) = 0$$

$$x = 0, 4 \therefore (0, 6) \text{ and } (4, 10)$$

b



14 $2x^2 - 5x + 1 = 3x + k$

$$2x^2 - 8x + 1 - k = 0$$

for tangent, repeated root $\therefore b^2 - 4ac = 0$

$$\therefore 64 - 8(1 - k) = 0$$

$$k = -7$$

15 $x^2 + ax + 18 = 2 - 5x$

$$x^2 + (a + 5)x + 16 = 0$$

intersect at 2 points $\therefore b^2 - 4ac > 0$

$$\therefore (a + 5)^2 - 64 > 0$$

$$a^2 + 10a - 39 > 0$$

$$(a + 13)(a - 3) > 0$$

$$a < -13 \text{ or } a > 3$$

16 a $x^2 - 2x + 6 = px + p$

$$x^2 - (p + 2)x + 6 - p = 0$$

for tangent, repeated root $\therefore b^2 - 4ac = 0$

$$\therefore (p + 2)^2 - 4(6 - p) = 0$$

$$p^2 + 8p - 20 = 0$$

$$(p + 10)(p - 2) = 0$$

$$p = -10, 2$$

b $x^2 - 2x + 6 = qx + 7$

$$x^2 - (q + 2)x - 1 = 0$$

for tangent, repeated root $\therefore b^2 - 4ac = 0$

$$\Rightarrow (q + 2)^2 + 4 = 0$$

but for real $q, (q + 2)^2 \geq 0 \therefore$ no solutions