

1 a $4x^2 - 9x + 5 = 3x - 4$

$$4x^2 - 12x + 9 = 0$$

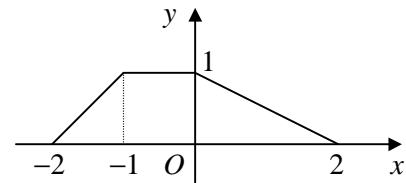
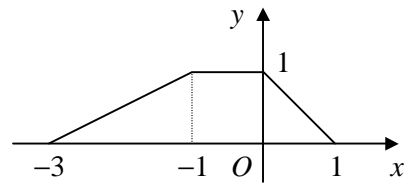
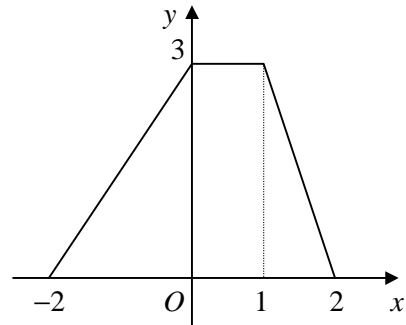
$$(2x - 3)^2 = 0$$

$$x = \frac{3}{2}$$

$$\therefore x = \frac{3}{2}, y = \frac{1}{2}$$

b $y = 3x - 4$ is a tangent to the curve
 $y = 4x^2 - 9x + 5$ at the point $(\frac{3}{2}, \frac{1}{2})$

2 a



3 a $x^2 + 5x + 2 = 4x + 1$

$$x^2 + x + 1 = 0$$

$$b^2 - 4ac = 1 - 4 = -3$$

$$b^2 - 4ac < 0 \therefore \text{no real roots}$$

\therefore does not intersect

b $x^2 + 5x + 2 = mx + 1$

$$x^2 + (5 - m)x + 1 = 0$$

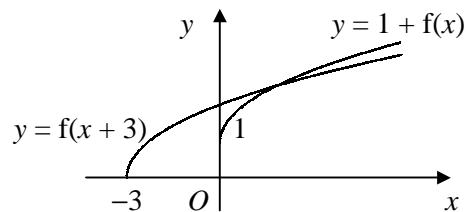
only one root $\therefore b^2 - 4ac = 0$

$$(5 - m)^2 - 4 = 0$$

$$5 - m = \pm 2$$

$$m = 3 \text{ or } 7$$

4 a



b $1 + \sqrt{x} = \sqrt{x+3}$

$$(1 + \sqrt{x})^2 = x + 3$$

$$1 + 2\sqrt{x} + x = x + 3$$

$$\sqrt{x} = 1$$

$$x = 1 \therefore (1, 2)$$

5 $x^2 + kx - 3 = k - x$

$$x^2 + (k+1)x - (k+3) = 0$$

$$b^2 - 4ac = (k+1)^2 + 4(k+3)$$

$$= k^2 + 6k + 13$$

$$= (k+3)^2 - 9 + 13$$

$$= (k+3)^2 + 4$$

real $k \Rightarrow (k+3)^2 \geq 0$

$$\Rightarrow (k+3)^2 + 4 \geq 4$$

$$\therefore b^2 - 4ac > 0$$

\Rightarrow real and distinct roots

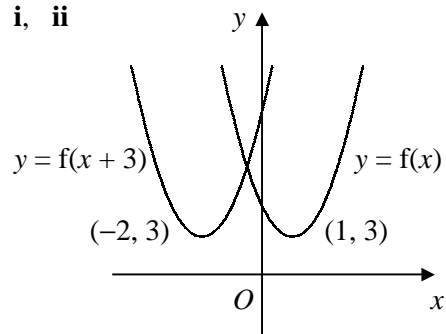
$\therefore l$ intersects C at exactly two points

6 a $f(x) = 2[x^2 - 2x] + 5$

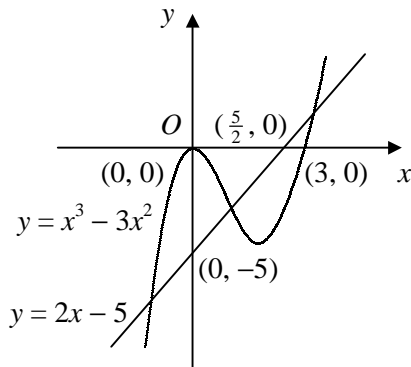
$$= 2[(x-1)^2 - 1] + 5$$

$$= 2(x-1)^2 + 3$$

b i, ii



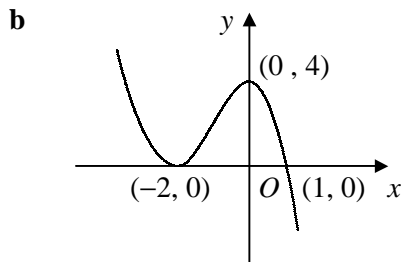
7 a $y = x^3 - 3x^2 = x^2(x - 3)$



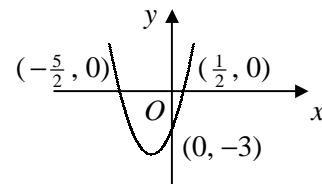
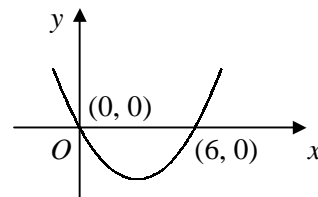
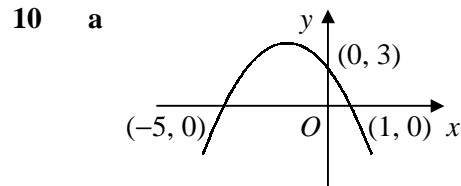
b 3 real roots

$x^3 - 3x^2 - 2x + 5 = 0 \Rightarrow x^3 - 3x^2 = 2x - 5$
 the graphs of $y = x^3 - 3x^2$ and $y = 2x - 5$
 intersect at three points

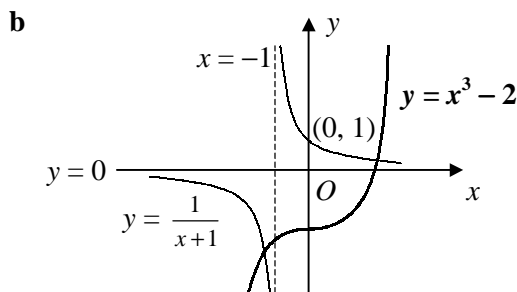
9 a LHS = $(1 - x)(2 + x)^2$
 $= (1 - x)(4 + 4x + x^2)$
 $= (4 + 4x + x^2) - x(4 + 4x + x^2)$
 $= 4 + 4x + x^2 - 4x - 4x^2 - x^3$
 $= 4 - 3x^2 - x^3$
 $= \text{RHS}$



8 touches x -axis at $(2, 0)$
 $\therefore y = k(x - 2)^2$
 crosses y -axis at $(0, -6)$
 $\therefore -6 = 4k$
 $k = -\frac{3}{2}$
 $\therefore y = -\frac{3}{2}(x - 2)^2$
 $y = -\frac{3}{2}x^2 + 6x - 6$
 $\therefore a = -\frac{3}{2}, b = 6$ and $c = -6$



11 a translation by 1 unit in the negative x -direction



c $x^3 - \frac{1}{x+1} = 2 \Rightarrow x^3 - 2 = \frac{1}{x+1}$
 the graphs $y = x^3 - 2$ and $y = \frac{1}{x+1}$ intersect
 at one point for $x > 0$ and at one point for $x < 0$
 \therefore one positive and one negative real root