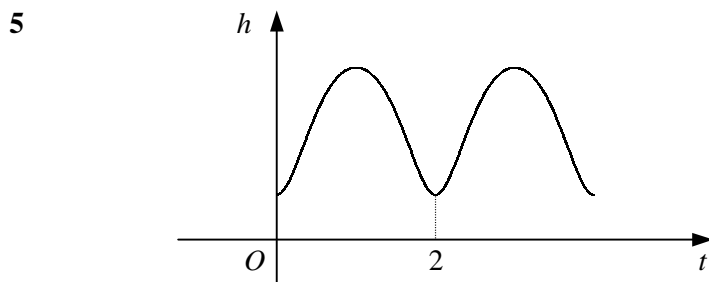


- 1 $f(x) \equiv 2x^3 + 5x^2 - 1$.
- Find $f'(x)$.
 - Find the set of values of x for which $f(x)$ is increasing.
- 2 The curve C has the equation $y = x^3 - x^2 + 2x - 4$.
- Find an equation of the tangent to C at the point $(1, -2)$. Give your answer in the form $ax + by + c = 0$, where a , b and c are integers.
 - Prove that the curve C has no stationary points.
- 3 A curve has the equation $y = \sqrt{x} + \frac{4}{x}$.
- Find $\frac{dy}{dx}$ and $\frac{d^2y}{dx^2}$.
 - Find the coordinates of the stationary point of the curve and determine its nature.
- 4 $f(x) \equiv x^3 + 6x^2 + 9x$.
- Find the coordinates of the points where the curve $y = f(x)$ meets the x -axis.
 - Find the set of values of x for which $f(x)$ is decreasing.
 - Sketch the curve $y = f(x)$, showing the coordinates of any stationary points.



The graph shows the height, h cm, of the letters on a website advert t seconds after the advert appears on the screen.

For t in the interval $0 \leq t \leq 2$, h is given by the equation

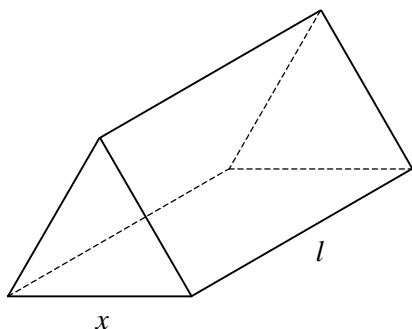
$$h = 2t^4 - 8t^3 + 8t^2 + 1.$$

For larger values of t , the variation of h over this interval is repeated every 2 seconds.

- Find $\frac{dh}{dt}$ for t in the interval $0 \leq t \leq 2$.
 - Find the rate at which the height of the letters is increasing when $t = 0.25$
 - Find the maximum height of the letters.
- 6 The curve C has the equation $y = x^3 + 3kx^2 - 9k^2x$, where k is a non-zero constant.
- Show that C is stationary when

$$x^2 + 2kx - 3k^2 = 0.$$
 - Hence, show that C is stationary at the point with coordinates $(k, -5k^3)$.
 - Find, in terms of k , the coordinates of the other stationary point on C .

7



The diagram shows a solid triangular prism. The cross-section of the prism is an equilateral triangle of side x cm and the length of the prism is l cm.

Given that the volume of the prism is 250 cm^3 ,

- find an expression for l in terms of x ,
- show that the surface area of the prism, $A \text{ cm}^2$, is given by

$$A = \frac{\sqrt{3}}{2} \left(x^2 + \frac{2000}{x} \right).$$

Given that x can vary,

- find the value of x for which A is a minimum,
- find the minimum value of A in the form $k\sqrt{3}$,
- justify that the value you have found is a minimum.

8

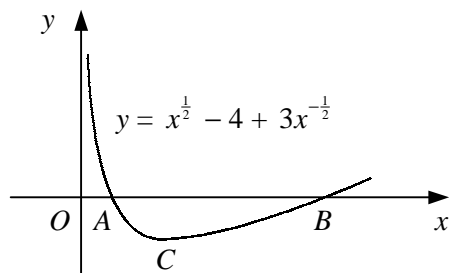
$$f(x) \equiv x^3 + 4x^2 + kx + 1.$$

- Find the set of values of the constant k for which the curve $y = f(x)$ has two stationary points.

Given that $k = -3$,

- find the coordinates of the stationary points of the curve $y = f(x)$.

9



The diagram shows the curve with equation $y = x^{\frac{1}{2}} - 4 + 3x^{-\frac{1}{2}}$. The curve crosses the x -axis at the points A and B and has a minimum point at C .

- Find the coordinates of A and B .
- Find the coordinates of C , giving its y -coordinate in the form $a\sqrt{3} + b$, where a and b are integers.

10

$$f(x) = x^3 - 3x^2 + 4.$$

- Show that $(x + 1)$ is a factor of $f(x)$.
- Fully factorise $f(x)$.
- Hence state, with a reason, the coordinates of one of the turning points of the curve $y = f(x)$.
- Using differentiation, find the coordinates of the other turning point of the curve $y = f(x)$.