

- 5 a** $2 \cos \frac{3x+x}{2} \sin \frac{3x-x}{2} = 0$
 $\cos 2x \sin x = 0$
 $\cos 2x = 0$ or $\sin x = 0$
 $2x = \frac{\pi}{2}, 2\pi - \frac{\pi}{2}$ or $x = 0, \pi$
 $2x = \frac{\pi}{2}, \frac{3\pi}{2}$ or $x = 0, \pi$
 $x = 0, \frac{\pi}{4}, \frac{3\pi}{4}, \pi$
- b** $\cos 4x - \cos x = 0$
 $-2 \sin \frac{4x+x}{2} \sin \frac{4x-x}{2} = 0$
 $\sin \frac{5}{2}x \sin \frac{3}{2}x = 0$
 $\sin \frac{5}{2}x = 0$ or $\sin \frac{3}{2}x = 0$
 $\frac{5}{2}x = 0, \pi, 2\pi$ or $\sin \frac{3}{2}x = 0, \pi$
 $x = 0, \frac{2\pi}{5}, \frac{2\pi}{3}, \frac{4\pi}{5}$
- c** $\cos(x-5x) - \cos(x+5x) = \cos 4x$
 $\cos(-4x) - \cos 6x = \cos 4x$
 $\cos 4x - \cos 6x = \cos 4x$
 $\cos 6x = 0$
 $6x = \frac{\pi}{2}, 2\pi - \frac{\pi}{2}, 2\pi + \frac{\pi}{2},$
 $4\pi - \frac{\pi}{2}, 4\pi + \frac{\pi}{2}, 6\pi - \frac{\pi}{2}$
 $= \frac{\pi}{2}, \frac{3\pi}{2}, \frac{5\pi}{2}, \frac{7\pi}{2}, \frac{9\pi}{2}, \frac{11\pi}{2}$
 $x = \frac{\pi}{12}, \frac{\pi}{4}, \frac{5\pi}{12}, \frac{7\pi}{12}, \frac{3\pi}{4}, \frac{11\pi}{12}$
- d** $4[\sin(2x + \frac{\pi}{2}) - \sin \frac{\pi}{6}] = 1$
 $\sin(2x + \frac{\pi}{2}) - \frac{1}{2} = \frac{1}{4}$
 $\sin(2x + \frac{\pi}{2}) = \frac{3}{4}$
 $2x + \frac{\pi}{2} = \pi - 0.8481, 2\pi + 0.8481$
 $= 2.2935, 7.1312$
 $2x = 0.7227, 5.5605$
 $x = 0.36, 2.78$
- e** $2 \sin \frac{x+\frac{x}{2}}{2} \cos \frac{x-\frac{x}{2}}{2} = 0$
 $\sin \frac{3}{4}x \cos \frac{1}{4}x = 0$
 $\sin \frac{3}{4}x = 0$ or $\cos \frac{1}{4}x = 0$
 $\frac{3}{4}x = 0$ or (none in interval)
 $x = 0$
- f** $2 \cos \frac{3x+x}{2} \cos \frac{3x-x}{2} = \cos 2x$
 $2 \cos 2x \cos x = \cos 2x$
 $\cos 2x(2 \cos x - 1) = 0$
 $\cos 2x = 0$ or $\cos x = \frac{1}{2}$
 $2x = \frac{\pi}{2}, 2\pi - \frac{\pi}{2}$ or $x = \frac{\pi}{3}$
 $2x = \frac{\pi}{2}, \frac{3\pi}{2}$ or $x = \frac{\pi}{3}$
 $x = \frac{\pi}{4}, \frac{\pi}{3}, \frac{3\pi}{4}$
- 6 a** $\cos(2x+3x) + \cos(2x-3x) - \cos x = 0$
 $\cos 5x + \cos(-x) - \cos x = 0$
 $\cos 5x + \cos x - \cos x = 0$
 $\cos 5x = 0$
 $5x = 90, 360 - 90, 360 + 90,$
 $720 - 90, 720 + 90$
 $= 90, 270, 450, 630, 810$
 $x = 18^\circ, 54^\circ, 90^\circ, 126^\circ, 162^\circ$
- b** $2 \cos \frac{3x+2x}{2} \sin \frac{3x-2x}{2} = 0$
 $\cos \frac{5}{2}x \sin \frac{1}{2}x = 0$
 $\cos \frac{5}{2}x = 0$ or $\sin \frac{1}{2}x = 0$
 $\frac{5}{2}x = 90, 360 - 90, 360 + 90$ or $\frac{1}{2}x = 0$
 $\frac{5}{2}x = 90, 270, 450$ or $\frac{1}{2}x = 0$
 $x = 0, 36^\circ, 108^\circ, 180^\circ$

$$\begin{aligned} \text{c } 2 \sin \frac{4x+2x}{2} \cos \frac{4x-2x}{2} &= \sin 3x \\ 2 \sin 3x \cos x &= \sin 3x \\ \sin 3x(2 \cos x - 1) &= 0 \\ \sin 3x = 0 \text{ or } \cos x &= \frac{1}{2} \\ 3x = 0, 180, 360, 540 \text{ or } x &= 60 \\ x = 0, 60^\circ, 120^\circ, 180^\circ \end{aligned}$$

$$\begin{aligned} \text{e } \frac{1}{2} [\sin(5x+x) - \sin(5x-x)] + \sin 4x &= 0 \\ \frac{1}{2} \sin 6x - \frac{1}{2} \sin 4x + \sin 4x &= 0 \\ \frac{1}{2} \sin 6x + \frac{1}{2} \sin 4x &= 0 \\ \sin \frac{6x+4x}{2} \cos \frac{6x-4x}{2} &= 0 \\ \sin 5x \cos x &= 0 \\ \sin 5x = 0 \text{ or } \cos x &= 0 \\ 5x = 0, 180, 360, 540, 720, 900 \text{ or } x &= 90 \\ x = 0, 36^\circ, 72^\circ, 90^\circ, 108^\circ, 144^\circ, 180^\circ \end{aligned}$$

$$\begin{aligned} 7 \quad \text{a } \text{LHS} &= 2 \sin \frac{x+3x}{2} \cos \frac{x-3x}{2} + \sin 2x \\ &= 2 \sin 2x \cos(-x) + \sin 2x \\ &= 2 \sin 2x \cos x + \sin 2x \\ &= \sin 2x(2 \cos x + 1) \\ &= \text{RHS} \end{aligned}$$

$$\begin{aligned} \text{d } \cos 2x - \cos(x-60) &= 0 \\ -2 \sin \frac{3x-60}{2} \sin \frac{x+60}{2} &= 0 \\ \sin(\frac{3}{2}x - 30) \sin(\frac{1}{2}x + 30) &= 0 \\ \sin(\frac{3}{2}x - 30) = 0 \text{ or } \sin(\frac{1}{2}x + 30) &= 0 \\ \frac{3}{2}x - 30 = 0, 180 \text{ or (none in interval)} \\ \frac{3}{2}x = 30, 210 \\ x = 20^\circ, 140^\circ \end{aligned}$$

$$\begin{aligned} \text{f } 2 \sin \frac{x+3x}{2} \cos \frac{x-3x}{2} &= 2 \cos \frac{x+3x}{2} \cos \frac{x-3x}{2} \\ \sin 2x \cos(-x) &= \cos 2x \cos(-x) \\ \sin 2x \cos x &= \cos 2x \cos x \\ \cos x(\sin 2x - \cos 2x) &= 0 \\ \cos x = 0 \text{ or } \sin 2x &= \cos 2x \\ \cos x = 0 \text{ or } \tan 2x &= 1 \\ x = 90 \text{ or } 2x = 45, 180 + 45 = 45, 225 \\ x = 22.5^\circ, 90^\circ, 112.5^\circ \end{aligned}$$

$$\begin{aligned} \text{b } \text{LHS} &= \frac{-2 \sin \frac{x+3x}{2} \sin \frac{x-3x}{2}}{2 \cos \frac{x+3x}{2} \cos \frac{x-3x}{2}} \\ &= \frac{-\sin 2x \sin(-x)}{\cos 2x \cos(-x)} \\ &= \frac{\sin 2x \sin x}{\cos 2x \cos x} \\ &= \tan x \tan 2x \\ &= \text{RHS} \end{aligned}$$