

9 a $\frac{dy}{dx} = -2x$, grad = 6

$$\therefore y + 6 = 6(x + 3)$$

$$y + 6 = 6x + 18$$

$$6x - y + 12 = 0$$

c $\frac{dy}{dx} = 4x + 5$, grad = 7

$$\therefore y - 2 = 7(x - \frac{1}{2})$$

$$2y - 4 = 14x - 7$$

$$14x - 2y - 3 = 0$$

10 a $\frac{dy}{dx} = 2x$, grad = 2

$$\therefore \text{grad of normal} = -\frac{1}{2}$$

$$\therefore y + 3 = -\frac{1}{2}(x - 1)$$

$$2y + 6 = -x + 1$$

$$x + 2y + 5 = 0$$

c $\frac{dy}{dx} = 3x^2 - 8$, grad = 4

$$\therefore \text{grad of normal} = -\frac{1}{4}$$

$$\therefore y + 4 = -\frac{1}{4}(x - 2)$$

$$4y + 16 = -x + 2$$

$$x + 4y + 14 = 0$$

11 a $x = 2 \therefore y = 4$

$$\frac{dy}{dx} = 6x - 5, \text{ grad} = 7$$

$$\therefore y - 4 = 7(x - 2)$$

$$y = 7x - 10$$

b $x = -3 \therefore y = 6$

$$\frac{dy}{dx} = 3x^2 + 10x, \text{ grad} = -3$$

$$\therefore \text{grad of normal} = \frac{1}{3}$$

$$\therefore y - 6 = \frac{1}{3}(x + 3)$$

$$y = \frac{1}{3}x + 7$$

13 a $\frac{dy}{dx} = 2x - 3$, grad = 1

$$\therefore \text{grad of normal} = -1$$

$$\therefore y - 2 = -(x - 2) \quad [y = 4 - x]$$

b $x^2 - 3x + 4 = 4 - x$

$$x^2 - 2x = 0$$

$$x(x - 2) = 0$$

$$x = 2 \text{ (at A) or } 0$$

$$\therefore B(0, 4)$$

b $\frac{dy}{dx} = -2x^{-2}$, grad = $-\frac{1}{2}$

$$\therefore y - 1 = -\frac{1}{2}(x - 2)$$

$$2y - 2 = -x + 2$$

$$x + 2y - 4 = 0$$

d $\frac{dy}{dx} = 1 - \frac{3}{2}x^{-\frac{1}{2}}$, grad = $\frac{1}{4}$

$$\therefore y + 2 = \frac{1}{4}(x - 4)$$

$$4y + 8 = x - 4$$

$$x - 4y - 12 = 0$$

b $\frac{dy}{dx} = 6x + 7$, grad = -5

$$\therefore \text{grad of normal} = \frac{1}{5}$$

$$\therefore y - 5 = \frac{1}{5}(x + 2)$$

$$5y - 25 = x + 2$$

$$x - 5y + 27 = 0$$

d $\frac{dy}{dx} = 1 + 6x^{-2}$, grad = $\frac{5}{3}$

$$\therefore \text{grad of normal} = -\frac{3}{5}$$

$$\therefore y - 1 = -\frac{3}{5}(x - 3)$$

$$5y - 5 = -3x + 9$$

$$3x + 5y - 14 = 0$$

12 a $\frac{dy}{dx} = 3x^2 + 6x - 16$, grad = 8

$$\therefore y + 10 = 8(x - 2) \quad [y = 8x - 26]$$

b $3x^2 + 6x - 16 = 8$

$$x^2 + 2x - 8 = 0$$

$$(x + 4)(x - 2) = 0$$

$$x = 2 \text{ (at P) or } -4$$

$$\therefore Q(-4, 50)$$

14 a $f'(x) = 3x^2 + 8x$

b $x = -3 \therefore y = -9$

$$\text{grad} = 3$$

$$\therefore y + 9 = 3(x + 3)$$

$$y = 3x \text{ which passes through } (0, 0)$$

$$15 \quad \mathbf{a} \quad y = 0 \Rightarrow 6 + x - x^2 = 0$$

$$(2 + x)(3 - x) = 0$$

$$x = -2, 3$$

+ve x -axis $\therefore P(3, 0)$

$$x = 0 \Rightarrow y = 6 \therefore Q(0, 6)$$

$$\mathbf{b} \quad \frac{dy}{dx} = 1 - 2x$$

grad at $P = -5$

$$y = -5(x - 3) \quad [y = 15 - 5x]$$

\mathbf{c} grad at $Q = 1$

tangent at Q : $y = x + 6$

$$\therefore 15 - 5x = x + 6$$

$$x = \frac{3}{2}$$

$$\therefore \left(\frac{3}{2}, \frac{15}{2}\right)$$

$$16 \quad \mathbf{a} \quad \text{grad of } l = -3$$

for curve, $\frac{dy}{dx} = 2x - 5$

$$\therefore \text{at } A, \quad 2x - 5 = -3$$

$$x = 1$$

$$\therefore A(1, -1)$$

$$\mathbf{b} \quad y + 1 = -3(x - 1)$$

$$y = -3x + 2$$

$$17 \quad \text{grad of normal} = 2$$

$$\therefore \text{grad of curve} = -\frac{1}{2}$$

for curve, $\frac{dy}{dx} = -32x^{-3}$

$$\therefore -\frac{32}{x^3} = -\frac{1}{2}$$

$$x^3 = 64$$

$$x = 4 \therefore (4, 1)$$

$$\text{sub. } 1 = 8 + k$$

$$k = -7$$