

1 $\frac{20 - 25}{\sigma} = \Phi^{-1}(0.25) = -0.674$ $\sigma = 5 \div 0.674$ $= 7.42$	M1 B1 M1 A1	4 Standardise and equate to Φ^{-1} [not .7754 or .5987] z in range [-0.675, -0.674], allow + (\pm) 5 \div z-value [not $\Phi(z)$ or 0.75] Answer in range [7.41, 7.42], no sign fudges [SR: σ^2 : M1B1M0A0 cc: M1B1M1A0]
2 P (1.2) Tables or correct formula used 0.8795	B1 M1 A1	3
3 (i) <i>Two of:</i> Distribution symmetric No substantial truncation Unimodal/Increasingly unlikely further from μ , etc <hr/> (ii) Variance $8^2/20$ $z = \frac{47.0 - 50.0}{\sqrt{8^2 / 20}} = -1.677$ $\Phi(1.677) = 0.9532$	B1 B1 <hr/> M1 A1 A1 A1	2 One property Another definitely different property Don't give both marks for just these two "Bell-shaped": B1 only unless "no truncation" <hr/> Standardise, allow cc, don't need n Denominator (8 or 8^2 or $\sqrt{8}$) \div (20 or $\sqrt{20}$ or 20^2) z-value, a.r.t. - 1.68 or +1.68 4 Answer, a.r.t. 0.953

4	() (a)	$\frac{15.0-20.0}{\sigma} = -0.253$	M1	For standardising and equating to $\Phi^{-1}(p)$
			B1	For correct value 0.253 (or 0.254) seen
		Hence $\sigma = \frac{5}{0.253} \approx 19.8$	M1	For solving equation for σ
			A1	4 For correct value 19.8
	(b)	$g = 25.0$, using symmetry	B1	For stating (or finding) the value of g
		Hence $P(G > 2g) = 1 - \Phi\left(\frac{50.0 - 20.0}{19.8}\right)$	M1	For correct process for upper tail prob
		$= 1 - 0.935 = 0.065$	A1	3 For correct answer
	(ii)	If normal, $P(G < 0)$ is substantial	M1	For considering relevant normal probability
		Hence the assumption seems unjustified	A1	2 For stating the appropriate conclusion

Question		Answer	Marks		Guidance
5		$\frac{150 - \mu}{\sigma} = 2.00$ $\frac{143 - \mu}{\sigma} = -1.5$ Solve to get $\mu = 146, \sigma = 2$	M1 A1 B1 M1 A1 A1 6	Standardise with σ, μ at least once, ignore cc, $\sqrt{\quad}$ errors, equate to z Both LHS and signs of RHS correct Both z -values correct to 3 SF Correct method for solution $\mu \in [145.95, 146.05)$ www $\sigma \in [1.995, 2.005)$ or $\sigma^2 = 4$ www	z not used, e.g. equated to 0.0228 and 0.9332 or 0.5092 and 0.8246: max M0M1 One z , one not: M1A0B0 Withhold if elimination done wrongly $\sqrt{\sigma}$ or σ^2 : can get M1A0B1M1A1A0 cc: M1A0B1M1A0A0

(6a)	$X \sim N(42, 3^2)$ $P(X > 50.0) = P\left(Z > \frac{50.0 - 42.0}{3.0}\right)$ $= P(Z > 2.667)$ $= 1 - \Phi(2.667) = 1 - 0.9962$ $= 0.0038$	M1 for standardizing M1 for prob. calc. with correct tail A1 NB answer given	3
(6b)	$P(\text{not positive}) = 0.9962$ $P(\text{At least one is out of 7 is positive})$ $= 1 - 0.9962^7 = 1 - 0.9737$ $= 0.0263$	B1 for use of 0.9962 in binomial expression M1 for correct method A1 CAO	3
(6c)	<p>If an innocent athlete is tested 7 times in a year there is a reasonable possibility (1 in 40 chance) of testing positive. Thus it is likely that a number of innocent athletes may come under suspicion and suffer a suspension so the penalty could be regarded as unfair. <i>Or</i> this is a necessary evil in the fight against performance enhancing drugs in sport.</p>	E1 comment on their probability in (i) B E1 for sensible contextual conclusion consistent with first comment	2
(6d)	$B(1000, 0.0038)$	B1 for B(,) or Binomial B1 <i>dep</i> for both parameters	2
(6e)	<p>A suitable approximating distribution is Poisson(3.8)</p> $P(\text{at least 10 positive tests})$ $= P(X \geq 10) = 1 - P(X \leq 9)$ $= 1 - 0.9942$ $= 0.0058$ <p><i>NB Do not allow use of Normal approximation.</i></p>	B1 for Poisson soi B1FT <i>dep</i> for $\lambda = 3.8$ M1 for attempt to use $1 - P(X \leq 9)$ A1 FT	4
(6f)	$P(\text{not testing positive}) = 0.995$ $\text{From tables } z = \Phi^{-1}(0.995) = 2.576$ $\frac{h - 48.0}{2.0} = 2.576$ $h = 48.0 + 2.576 \times 2.0 = 53.15$	B1 for 0.995 seen (or implied by 2.576) B1 for 2.576 (FT their 0.995) M1 for equation in h and positive z -value A1 CAO	4
			18

7. 0.677 (6)

8a. 0.126 (3)

8b. 0.281 (6)

9a. 0.298 (3)

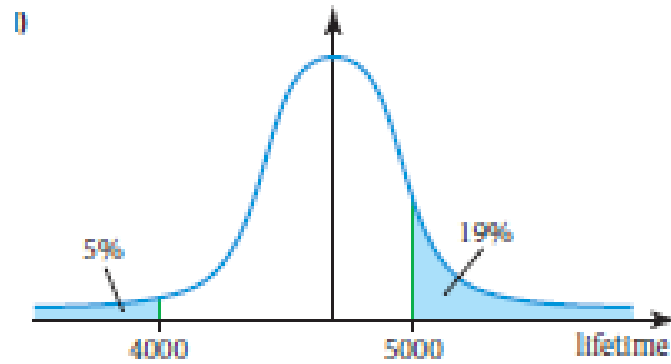
9b. 0.118 (6)

9c. 13 (3)

10a. 8.75 (4)

10b. 0.546 (3)

11a.



(2)

11b. $\mu = 4650$

(2)

11c. 0.44 (2 s.f.)

(3)

11d. 3700 hours

(3)

11e. 0.76 (2 s.f.)

(3)